

Chapter 2

Reasoning and Proofs



2.1 - Conditional Statements

2.2 - Inductive and Deductive Reasoning

2.3 - Postulates and Diagrams

2.4 - Algebraic Reasoning

2.5 - Proving Statements about Segments and Angles

2.6 - Proving Geometric Relationships

2.6 - Proving Geometric Relationships

Theorems

Right Angles Congruence Theorem

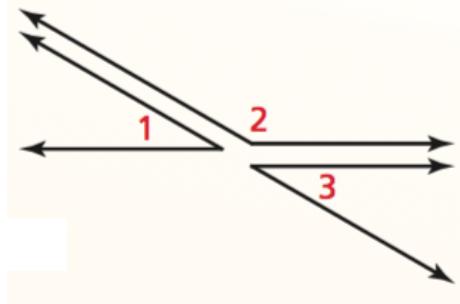
All right angles are congruent.



$$\angle 1 \cong \angle 2$$

Congruent Supplements Theorem

If two angles are supplementary to the same angle, then they are congruent.



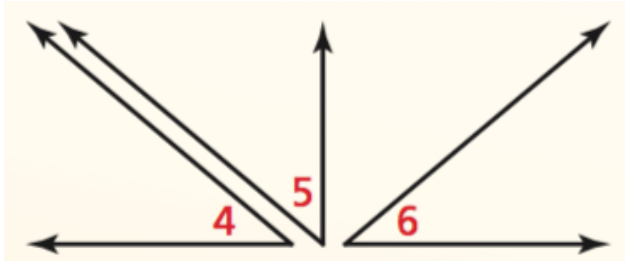
If $\angle 1$ is supplementary to $\angle 2$
and $\angle 3$ is supplementary to $\angle 2$,
then $\angle 1 \cong \angle 3$.

2.6 - Proving Geometric Relationships

Theorems

Congruent Complements Theorem

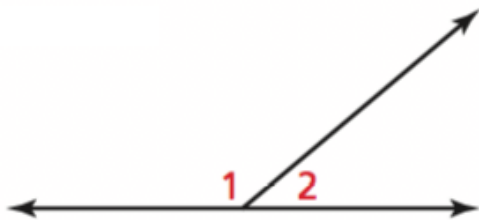
If two angles are complementary to the same angle, then they are congruent.



If $\angle 4$ is complementary to $\angle 5$
and $\angle 6$ is complementary to $\angle 5$,
then $\angle 4 \cong \angle 6$.

Linear Pair Postulate

If two angles for a linear pair, then they are supplementary.



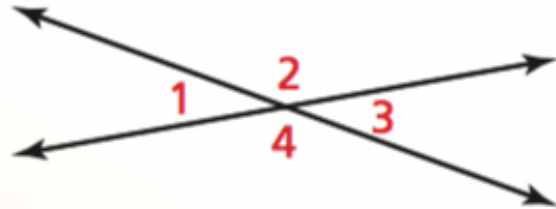
If $\angle 1$ and $\angle 2$ form a linear pair,
then $\angle 1$ and $\angle 2$ are supplementary.

2.6 - Proving Geometric Relationships

Theorems

Vertical Angles Theorem

Vertical angles are congruent.

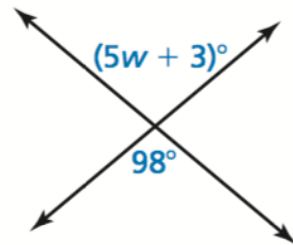


$$\angle 1 \cong \angle 3$$

$$\angle 2 \cong \angle 4$$

Compute the angles:

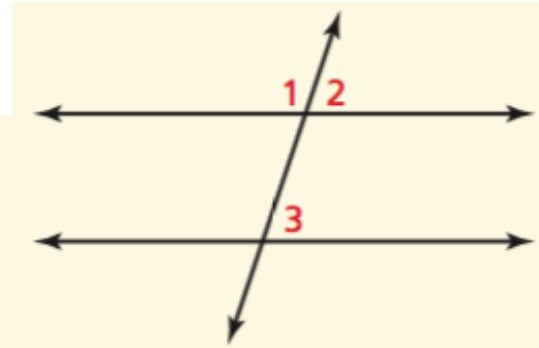
- 1) If $m\angle 1 = 53^\circ$ above, compute the values of angles 2, 3, and 4.
- 2) Compute the value of w in the diagram below.



2.6 - Proving Geometric Relationships

Complete the proof:

Given $\angle 1$ and $\angle 2$ are supplementary.
 $\angle 1$ and $\angle 3$ are supplementary.
Prove $\angle 2 \cong \angle 3$



Statement

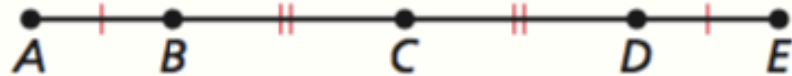
Reason

2.6 - Proving Geometric Relationships

Complete the proof:

Given $AB = DE, BC = CD$

Prove $\overline{AC} \cong \overline{CE}$



STATEMENTS

1. $AB = DE, BC = CD$
2. $AB + BC = BC + DE$
3. _____
4. $AB + BC = AC, CD + DE = CE$
5. _____
6. $\overline{AC} \cong \overline{CE}$

REASONS

1. Given
2. Addition Property of Equality
3. Substitution Property of Equality
4. _____
5. Substitution Property of Equality
6. _____